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FORM OF INSTABILITY OF STEADY CONVECTIVE MOVEMENT CAUSED BY INTERNAL HEAT SOURCES

by

A. A. Yakimov





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By: A. A. Yakimov

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Гr	r .	G, g	Уу	уу	U, u
Дд	Дд	D, d	Фф	0 0	F, f
Еe	E .	Ye, ye; E, e*	X ×	Xx	Kh, kh
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Пп	Пп	P, p	Яя	Яя	Ya, ya

*ye initially, after vowels, and after ъ, ь; e elsewhere. When written as \ddot{e} in Russian, transliterate as $y\ddot{e}$ or \ddot{e} .

RUSSIAN AND ENGLISH TRIGONOMETRIC FUNCTIONS

Russian	English	Russian	English	Russian	English
sin	sin	sh	sinh	arc sh	sinh-1
cos	cos	ch	cosh	arc ch	cosh_1
tg	tan	th	tanh	arc th	tanh_1
ctg	cot	cth	coth	arc cth	coth_i
sec	sec	sch	sech	arc sch	sech_1
cosec	csc	csch	csch	arc csch	csch

Russian English
rot curl
lg log

1233

FORM OF INSTABILITY OF STRADY CONVECTIVE MOVEMENT CAUSED BY INTERNAL REAT SCURCES

A. A. Yakinov

The stability of steady convective movement caused by internal heat scurces was studied earlier in [1, 2]. The spectra of the decrements of the disturbances and the neutral curves were obtained for different values of the Prandtl number. This report considers the form of the disturbances of convective novement.

1. Heat sources with volumetric density Q are uniformly distributed in a plane vertical layer of viscous fluid with a width of 2h. The layer is assumed to be closed from above and below, and the vertical walls which bound it are held at the same temperatures. Stationary plane-parallel convective movement with velocity and

temperature profiles which are even relative to the axis of the charnel, found from the ordinary equations of convection with consideration of internal heat sources [1], originate in this channel due to internal heating. If we take h, h^2/ν , $g\beta qh^4/2\nu$, $qh^2/2$, $\rho g\beta h^2/2$ ($q = Q/\rho c_{pX}$) as the units of distance, time, velocity, temperature, and pressure, respectively, the disensionless velocity and temperature profiles will be

$$v_0 = 1/60(1 - 6x^2 + 5x^4),$$
 (1)
 $T_0 = 1 - x^2.$ (2)

Small plane spread disturbances

$$\psi(x, z, t) = \varphi(x) \exp(-\lambda t + ikz), \tag{3}$$

$$T(x, z, t) = \theta(x) \exp(-\lambda t + ikz), \tag{4}$$

are imposed on the main flow, where ϕ and 6 are the amplitudes of the oscillations, λ is the decrement, and k is the wave number.

Substituting (3) and (4) in the convection equation and considering the smallness of the disturbances, we will obtain a system of linear homogeneous differential equations for determining intensities φ (x) and θ (x) [1]:

$$\Delta^{2}\varphi - ikGH\varphi + \theta' = -\lambda\Delta\varphi,$$

$$P^{-1}\Delta\theta + ikG(T_{0}'\varphi - v_{0}\theta) = -\lambda\theta$$

$$(\Delta\varphi \equiv \varphi'' - k^{2}\varphi, H\varphi \equiv v_{0}\Delta\varphi - v_{0}^{*}\varphi, G = g\beta qh^{5}/2v^{2}, P = v/\chi)$$

with the homogeneous boundary conditions

$$\varphi = \varphi' = 0, \ \theta = 0$$
 at $x = \pm 1$. (7)

2. We will use the Galerkin method to solve boundary problem (5)-(7). We will find of and 0 in the form of the basic functions

$$\varphi = \sum_{i=1}^{N} a_i \varphi_i, \quad \theta = \sum_{k=1}^{M} b_k \theta_k. \tag{8}$$

We will take the intensity of the disturbances in a quiescent fluid, determined from the boundary pochles

$$\Delta^2 \varphi_i = -\mu_i \Delta \varphi_i, \ \varphi_i = \varphi_i' = 0, \ \text{at} \ x = \pm 1,$$

$$(i = 1, 2, \dots, N),$$

$$(9)$$

as the basic functions ϕ_ℓ , and the intensity of the temperature perturbations, determined by the pighles

$$P^{-1}\Delta\theta_k + v_k\theta_k = 0, \quad \theta_k = 0 \quad \text{at} \quad x = \pm 1$$
 (10)
 $(k = 1, 2, \dots, M)$

as the basic functions θ_s (the explicit form of the basic functions is given in [3], for exemple).

The requirement of the orthogonality of the discrepancies in the tasic functions leads to a system of boundaries alignment algebraic equations for coefficients a_i and b_k .

The condition of the existence of a nonzero solution for this system determines the spectrum of the characteristic decrements of disturtances λ depending on the Grashof number N, the Prandtl number F and the wave number k. The characteristic decrements λ are defined as the intrinsic values of the system matrix.

The expansion coefficients are the contenents of the latent vector which corresponds to characteristic number λ . This vector was found as follows. The value of λ was substituted in the characteristic equation

 $|A - \lambda E| = 0. \tag{11}$

where A is the system matrix and B is the unit matrix. One equation was deleted from the system obtained. For the best conditionality of the matrix obtained, the equation with the minimum modulus of the coefficient in the diagonal term was selected as this equation. One of the unknowns $(a_k$ or b_k) was assigned a random value (e.g., "-1"), and the system thus obtained (with complex elements) was solved by the method of primary elements.

3. The normal disturbances ψ (x, z, t) and T(x, z, t) with a certain amplitude a, which remains arbitrary when staying within the hounds of the linear theory of stability, are added to the main flow and distort it. We will plot the current lines and isotherms of the disturbed total movement.

At an arbitrary fixed point in time t_0 , the equation of the current line of disturbed accesses is

$$\psi_0(x) + a\psi(x, z, t_0) = C_1,$$

where $\psi_0(x)$ is the current function of the primary flow, and C_1 is a certain constant.

If disturbances $\psi(x, 2, t)$ are determined from formula (3), the current line equation assumes the following form:

$$\psi_0(x) + a_1 \varphi(x) e^{ikz} = C_1.$$
 (12)

Factor $e^{\lambda t_0}$ quly affects the intensity of the disturbances; therefore, we can set $t_0 = 0$ without affecting continuity.

Considering the complex form of $\phi(x)$ and C_1 , equation (12) can be rewritten as:

$$\psi_0(x) + a_1 \left[\varphi_r(x) \cos kz - \varphi_1(x) \sin kz \right] = A_1, \tag{13}$$

where

$$\varphi_{i}(x) = Re\,\varphi(x), \ \varphi_{i}(x) = \operatorname{Im}\,\varphi(x).$$

and a, and A, are real constants.

The isolines are plotted as follows. The corresponding values of x are found from equation (13) for a given value of A, and a fixed value of x. Breaking down the change interval x into a sufficiently

large number of parts, we will obtain the current line for the selected value of 4. Varying 4, with a certain spacing, we will find the family of equidistant current lines. The equation for the isotherms

$$T_0(x) + a_1[\theta_r(x)\cos kz - \theta_l(x)\sin kz] = B_1,$$
 (14)

is found analogously, where

$$\theta_r(x) = Re\,\theta(x), \ \theta_l(x) = \operatorname{Im}\,\theta(x),$$

and the family of isotherns of the disturbed accement is plotted.

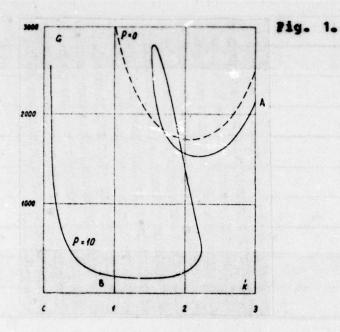
4. The results of the numerical calculations are given below.

The intrinsic values of the system matrix were found using the QR algorithm realized on Aragats and E-220H computers of the Computer Center of the Perm! State University [4]. Six to fifteen functions of each type were taken in expansions (8): The latent vector, isolines and isotherms were found on an H-220H computer.

Figure 1 shows the neutral curve for the Prandtl number P = 10 plotted from the materials in [2]. As this study establishes, at sufficiently large values of the Prandtl number, the neutral curve consists of two branches. The short-wave branch corresponds to hydrodynamic disturbances drifting slowly along the channel. The long-wave branch corresponds to heat wave disturbances, the phase velocity of which is close to the maximum flow velocity.

Fortnete: *For comparison, the broken line in Fig. 1 shows the peutral curve for P = 0 taken from [1], which characterizes the development of hydrodynamic disturbances alone. End footnote

It is interesting to trace the form of the disturbances corresponding to both branches.



Bigure 2 shows the current lines and isotherms of the total convective movement plotted for point A (see Fig. 1), which lies on the hydrodynamic branch of the neutral curve (k = 3; G = 2180). Figure 3 corresponds to point E, which is located on the thermal branch (k = 0.8; G = 230). For convemience of illustration, the vertical scale in this figure is one-fourth of the full scale.

Fig. 2. KBY: (1) Current lines. (2) Isotherns.

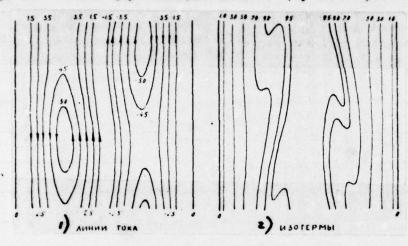
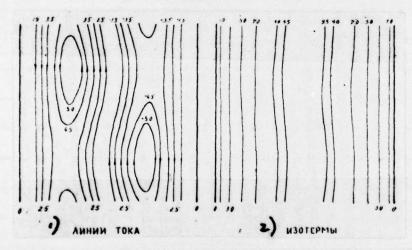


Fig. 3. KBY: (1) Current lines. (2) Isotherms.



The values of the current function indicated in the figures are increased 10³ times, and the temperature values - ten times. When comparing the figures one should remember that constant as used in formulae (13) and (14) was 2.5 times larger for point A than for point B when plotting the isolines.

These figures show that in both cases, instability develops in the ferm of two vortex chains which alternate on the interfaces of the convective flows. Thus, although hydrodynamic disturbances and rising heat flux disturbances are related to two different modes of the instability spectrum, there is no essential difference in their form. However, the difference is that heat waves have a relatively high phase velocity compared to hydrodynamic disturbances.

Eibliggraphy

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